

Nonequilibrium mechanical-electrochemical coupling in Li-ion batteries

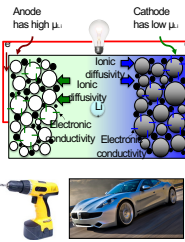
Hongjiang Chen and Hsiao-Ying Shadow Huang

Mechanical and Aerospace Engineering, North Carolina State University, Raleigh, NC

Introduction and Background

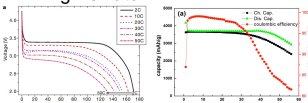
Introduction:

- Lithium-ion batteries are critical to modern and emerging technologies such as electric vehicles, high-power tools.
- It stores and release energy by Li-ion's diffusion between anode and cathode.

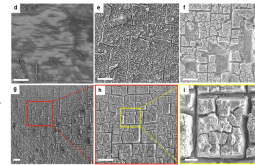


Current Problems of Li-ion battery

- (a) Poor power performance under high C-rate^[1]
- (b) Irreversible capacity loss after cycling and limited lifetime under high C-rate^[2]

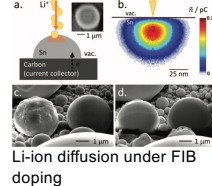


(c) Electrodes' cracks and failure^[3]

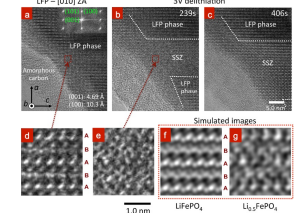


Si anode SEM images after (d) 3, (e) 8, (f) 50 and (g-i) 300 cycles. Scale bar, 20μm (d-h), 3 μm (i).

(d) Li-ion diffusion were affected by mechanical deformation^[4]



(e) Solid solution zone (SSZ) observed during non-equilibrium process^[5]



Objective:

- Describe and predict electrical potential, capacity, stress and strain under high C-rate (dis)charging.
- Present the relation between stress/strain and solid solution zone (SSZ) during non-equilibrium process
- Develop approaches to improve Li-ion battery's cyclic life at high C-rates

Methods and Current Results

Model Architecture based on Continuum Mechanics and Non-Equilibrium Thermodynamics

Constitutive models

$$\dot{\Omega} = \dot{\Omega}(\lambda, G, \rho, g, \dot{\epsilon}^{(e)}, \sigma, \dot{\epsilon}, \kappa, \chi_{(k)}, \dot{\epsilon}^{(e)})$$

$$\mu_{(12)} = \mu_{(12)}(\chi_{(k)}, \dot{\epsilon}^{(e)}, \rho)$$

$$ds = \sum_i \bar{\gamma}^{(i)} d\bar{\epsilon}_{(2ij)}^{(i)} + c_{vz} \frac{dT}{T} + \left(\frac{\partial s}{\partial \chi_{(k)}} \right) d\chi_{(k)}$$

Momentum equation

$$\rho \frac{d\mathbf{v}}{dt} = \nabla \cdot \mathbf{p} + \sum_k \rho_{(k)} \mathbf{F}_{(k)}$$

Dissipation models

$$\lambda^{(p)z} = C^{(p)z} \exp\left(-\frac{E_z^{(p)z}}{RT}\right)$$

$$\tau^{(e)} = \tau^{(e)}(\dot{\epsilon}^{(e)}, \lambda^{(p)z})$$

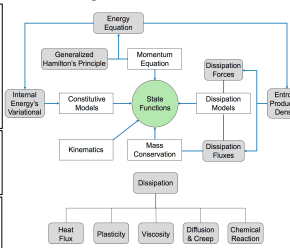
$$J_{(k)} = -\frac{J_{(k)}}{T} + \nabla T - \sum_k \frac{1}{T} \nabla \cdot (\mathbf{v}_{(k)} - \mathbf{v}_{(s)}) - \frac{J_{(k)}}{T} \nabla \phi$$

$$r_{(k)}^{(i)} = C_{(k)}^{(i)} \exp\left(\alpha^{(i)} \beta \sum_k \mu_{(k)} \delta^{(i)}\right)$$

Mass conservation

$$\rho \frac{d\chi_{(k)}}{dt} + \nabla \cdot \mathbf{J}_{(k)} = \sum_i \dot{\rho}_{(i)}^{(k)}$$

$$F_{(k)} \cdot \mathbf{J}_{(k)} dV = I$$



Kinematics

$$\dot{\epsilon}_{(2ij)} = \frac{\partial \epsilon_{(2ij)}}{\partial t} = \frac{1}{2} \frac{\partial \dot{\epsilon}_{(2ij)}}{\partial t}$$

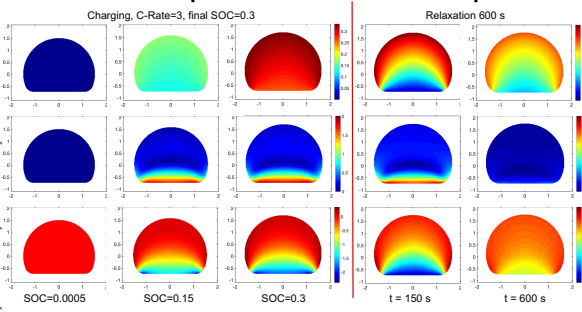
$$\dot{\epsilon}_{(2ij)} = \dot{\epsilon}_{(ij)}^{(e)} + \dot{\epsilon}_{(ij)}^{(p)}$$

$$\dot{\epsilon}_{(2ij)} = \frac{1}{2} (\nabla_i v_{(j)} + \nabla_j v_{(i)})$$

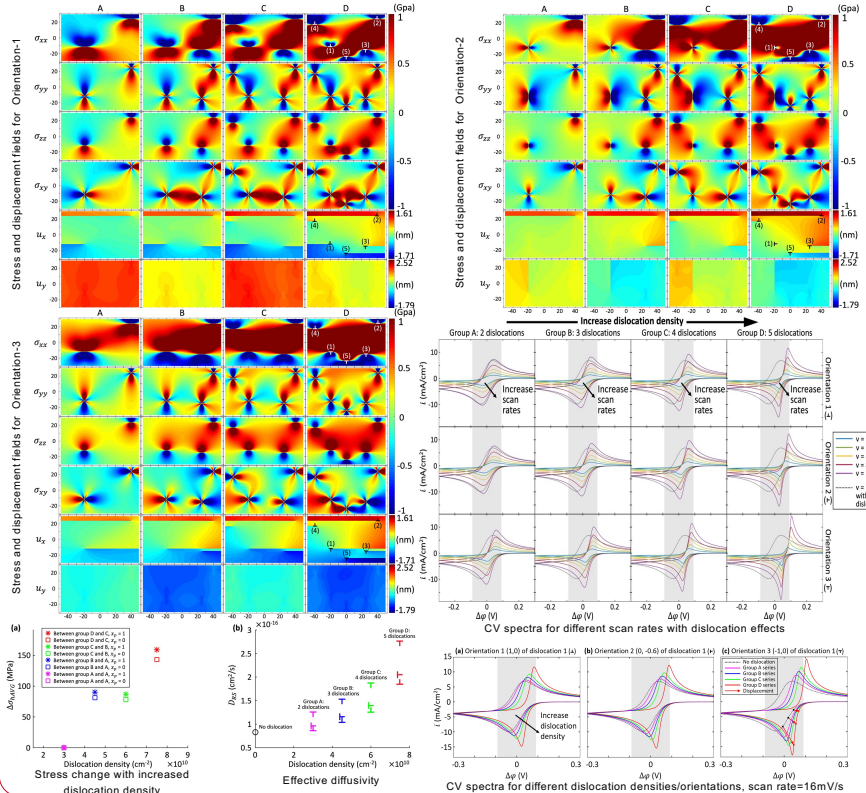
Dislocation effects

$$\sigma_{DC} = \sigma_{DC}(b_x, b_y, r_x, r_y) \quad \mathbf{u}_{DC} = \mathbf{u}_{DC}(b_x, b_y, r_x, r_y)$$

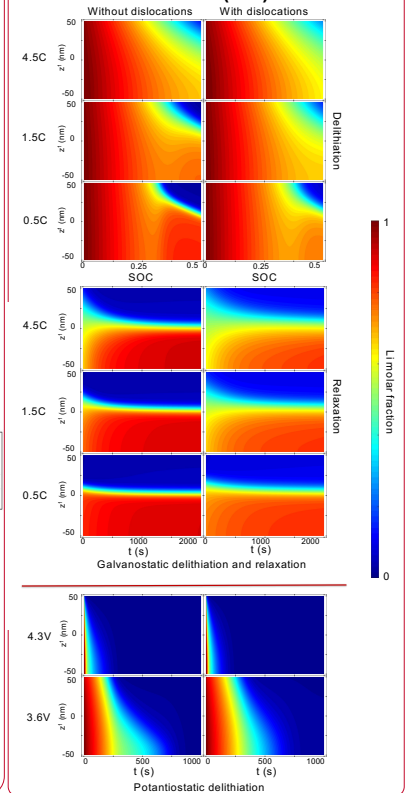
Li diffusion and particle deformation for Tin particle



Dislocation effects for LiFePO4



SSZ in LiFePO4 with(out) dislocations



Future Work

- Simulate whole (dis)charging process and cycling for large deformation of Si anode.
- Investigate the Influences of material's parameters on the evolution of SSZ. Multi-particle modeling.
- Damage and irreversible capacity loss modeling.

[1] Kang & Ceder, Nature 458, 190-193; [2] J. Xie et al, doi: 10.1149/2.0091503jes; [3] Shi et al, doi: 10.1038/ncomms11886; [4] Saya Takeuchi et al., doi:10.1149/2.1161606jes; [5] Niu et al., dx.doi.org/10.1021/nl501415w